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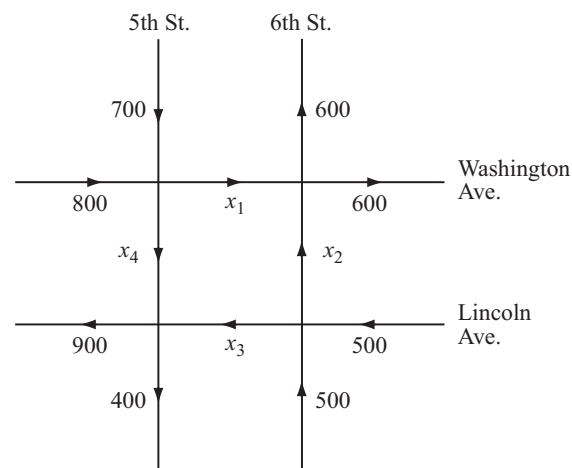
1 次の連立 1 次方程式を Gauss の消去法のアルゴリズムにしたがって解け.

$$\begin{cases} -2y - 3z - 6w = 1 \\ x - 3y + z - 2w = 1 \\ -2x + 7y + 8w = -2 \\ -3y - 4z - 9w = -1 \end{cases}$$

2 次の連立 1 次方程式が解を持つように定数  $a$  を決め, そのときの解をすべて求めよ.

$$\begin{cases} x + 3y + z - 2w = -2 \\ 2x + 7y - z - 6w = -3 \\ x + 2y + 7z + 3w = -6 \\ 4x + 9y + 7z - 8w = a \end{cases}$$

3 Traffic flow. The rush-hour traffic flow for a network of four one-way streets in a city is shown in the figure. The numbers next to each street indicate the number of vehicles per hour that enter and leave the network on that street. The variable  $x_1, x_2, x_3,$  and  $x_4$  represent the flow of traffic between the four intersections in the network.



- For a smooth traffic flow, the number of vehicles entering each intersection should always equal the number leaving. For example, since 1500 vehicles enter the intersection of 5th Street and Washington Avenue each hour and  $x_1 + x_4$  vehicles leave this intersection, we see that  $x_1 + x_4 = 1500$ . Find the equations determined by the traffic flow at each of the other three intersections.
- Find the solution to the system in a).
- What is the maximum number of vehicles that can travel from Washington Avenue to Lincoln Avenue on 5th Street? What is the minimum number?
- If traffic lights are adjusted so that 1000 vehicles per hour travel from Washington Avenue to Lincoln Avenue on 5th Street, determine the flow around the rest of the network.