Midterm Exam

1 a) Simplify the following 4A - 3(B - 2(C - 2(B - A))) =

b) Let
$$A = a^2 - ab - 2b^2$$
, $B = a^2 - 2ab + 3b^2$, $C = 3a^2 + 4ab - 5b^2$.
Simplify the following.
 $4A - 3(B - 2(C - 2(B - A))) =$

- 2 Expand the following expressions.
- a) $(3a 2b)^3 =$
- b) $(5a^2 2bc)(3a^2 4bc) =$
- c) $(x^2 + x + 1)(x^2 x + 1) =$
- **3** Factor the following expressions.
- a) $3x^2 4x 4 =$
- b) $4a^2 12ab + 9b^2 =$
- c) $18x^2 2y^2 =$
- d) $27x^3 y^3 =$

Find the greatest common divisor (GCD) and the least common multiple (LCM) of each of the following polynomials.

- a) a^2b^3 , a^4b^4c , $a^3b^2c^2$ GCD= LCM=
- b) $(x + 1)(x 1)^2$, $(x + 1)^2(x + 2)(x 1)$ GCD= LCM=
- 5 Using long division, find the quotient and the remainder.

$$2x^2 - x - 1$$
) $2x^4 + x^3 - 3x - 3$

- 6 Let $P(x) = x^3 5x^2 + 3x + 9$.
- a) Find the value P(-1).
- b) Factor the polynomial P(x).

Z Express the following fraction of polynomials as the sum of a polynomial and a fraction whose numerator has a degree less than its denominator.

a)
$$\frac{3x+1}{x+2} =$$

b)
$$\frac{x^2 - x - 1}{x - 3} =$$

8 Reduce each of the following fractions to its lowest terms.

a)
$$\frac{(-2x^2y)^3}{(-3x^3y^2)^2} =$$

b)
$$\frac{2x^2y^2}{6x^2y - 4xy^2} =$$

c)
$$\frac{a^3 - b^3}{a^3 - ab^2} =$$

9 Simplify the following expressions.

a)
$$\frac{12x}{\frac{3}{x}} =$$

b) $\left(-\frac{2xy^2}{a^2}\right) \div \left(-\frac{ay}{4x^2}\right) =$

c)
$$\frac{x^2 - x - 6}{x^2 + 4x + 4} \div \frac{x^2 - 5x + 6}{x^2 - 2x - 8} =$$

d)
$$\frac{a^2 - b^2}{(a-b)^2} \div \frac{a^2 - 2ab + b^2}{a^3 - a^2b + ab^2} \times \frac{a^2b + ab^2}{a^3 + b^3}$$

=

e)
$$\frac{b-c}{bc} + \frac{c-a}{ca} + \frac{a-b}{ab} =$$

f)
$$\frac{2x^2}{4x^2 - y^2} + \frac{x - y}{y - 2x} =$$

g)
$$\frac{x+2}{2x^2-x-1} + \frac{3x+2}{2x^2+3x+1} =$$

h)
$$\frac{a}{ab-b^2} + \frac{b}{ba-a^2} =$$

a)
$$\frac{x+4}{3} \ge 1-2x > \frac{x}{2} - \frac{2}{3}$$

b) $|3x + 2| \ge 5$

12 A group of people wants to create a team T-shirt for a sports festival. The usual price for a T-shirt is 1,000 yen per T-shirt, but if you pay the 4,000 yen fee, the member's price will be 850 yen per T-shirt. If you become a member, how many T-shirts you must buy to make the total amount cheaper.



i)
$$\frac{1}{x(x+1)} + \frac{1}{(x+1)(x+2)} + \frac{1}{(x+2)(x+3)} =$$



k)
$$\frac{2a}{1-\frac{1}{a}-\frac{1}{1+\frac{1}{a}}} =$$

10 Solve the following equation with respect to the unknown indicated in [].

a)
$$\frac{1}{p} + \frac{1}{q} = \frac{1}{r}$$
 [p]